

# Doubly Charged Leptons and The Higgs Portal

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# Motivation

- Higgs portal is very simple model that connects the dark matter sector to the SM via a SM singlet scalar  $\Phi$
- It is simple and independent of the details of the dark sector.
- It also very useful for electroweak baryogenesis.
- Being a SM singlet it is very difficult to probe.
- Need a systematic study to enhance its signal in both higher energy collider experiments as well as precision measurements and searches.

# Higgs Portal Lagrangian

The scalar potential for the scalar portal is

$$V = -\mu^2 H^\dagger H + \lambda(H^\dagger H)^2 + \lambda_\phi(\Phi^\dagger\Phi)^2 + M_\phi^2\Phi^\dagger\Phi + \lambda_{\phi h}\Phi^\dagger\Phi H^\dagger H + \alpha\Phi + \beta\Phi^\dagger\Phi\Phi + \kappa_H\Phi H^\dagger H + h.c.$$

where  $H$  is the SM Higgs field.

- $\kappa_H$  will induce a mixing with the Higgs
- If  $\Phi$  picks up a VeV  $\lambda_{\phi H}$  term will also gives rise to mixing with Higgs

## $\phi - h$ mixing

If  $\Phi$  is not Higgsed then the mixing is given by

$$\frac{1}{2} \begin{pmatrix} h & \phi \end{pmatrix} \begin{pmatrix} 2v^2\lambda & \frac{v\kappa_H}{\sqrt{2}} \\ \frac{v\kappa_H}{\sqrt{2}} & \bar{M}_\phi^2 \end{pmatrix} \begin{pmatrix} h \\ \phi \end{pmatrix},$$

where  $\bar{M}_\phi^2 = M_\phi^2 + \lambda_{\phi h} v^2/2$ .  $(h, \phi)$  is related to the mass eigenstates  $(h', \phi')$  by the usual  $2 \times 2$  rotation matrix define by the mixing angle  $\theta$  which is given by

$$\tan 2\theta = \frac{\sqrt{2}v\kappa_H}{\bar{M}_\phi^2 - v^2\lambda}.$$

From Higgs measurement we get  $\sin^2 \theta < .04$ .

Very small signature in Higgs measurements

# di-Higgs Boson Production

Use the process

$$g + g \rightarrow \phi \rightarrow h + h$$

This gives a possible enhancement over SM di-Higgs production for  $\phi \sim 300 - 400$  GeV. Needs high luminosity LHC.

# Enhance $\phi$ signature by vectorlike fermions

We need new states that carry SM quantum numbers and also couple to  $\Phi$

- Fermions are obvious candidates. Due to anomaly cancellations they have to be vectorlike
- Simplest are vectorlike leptons
- To go even further in simplicity examine  $SU(2)_I$  singlets.
- They need  $Y > 1$  in order not to mix with  $e_R$
- They narrow to  $E^{\pm\pm}$
- They can couple to  $\Phi$  by  $\bar{E}E\Phi$  coupling.
- They can also be searched for in  $e^+e^-$  colliders.

# $E^{\pm\pm}$ is not enough

As is written the lepton  $E^{\pm\pm}$  is stable.  
We have to make it decay.

$$E^{\pm\pm} \rightarrow W^{\pm} \ell^{\pm}, \quad \ell = e, \mu, \text{ or } \tau$$

is allowed by charge and angular momentum conservation.

Forbidden by  $SU(2)$

Simplest solution is to add a  $SU(2)_L$  singlet with  $Y = 1$  scalar.

Decay modes are

- If  $M_E > M_S$  2-body decay  $E^{++} \rightarrow S + \ell^+$
- If  $M_E < M_S$  3-body decay  $E^{++} \rightarrow \ell^+ + \ell'^+ + \nu$

# Particle Content of Minimal Model

The quantum numbers of the new particles together with the relevant SM fields are given in Table (1) below

**Table :** Quantum numbers of the SM Higgs  $H$ , leptons  $L, \ell$  and  $E, S, \phi$

Field	$SU(2)$	$U(1)_Y$
$H$	<b>2</b>	$\frac{1}{2}$
$L$	<b>2</b>	$-\frac{1}{2}$
$\ell_R$	<b>1</b>	$-1$
$E$	<b>1</b>	$-2$
$S$	<b>1</b>	$1$
$\phi$	<b>1</b>	$0$

where standard notations are used.

# New Lagrangian

$$\begin{aligned}\mathcal{L}' &= \bar{E}i\gamma^\mu(\partial_\mu - 2ig_1B_\mu)E + [(\partial^\mu + ig_1B^\mu)S]^\dagger(\partial_\mu + ig_1B_\mu)S \\ &- [f_{e\mu}(\bar{\nu}_e^c\mu_L - \bar{\nu}_\mu^c e_L) + f_{e\tau}(\bar{\nu}_e^c\tau_L - \bar{\nu}_\tau^c e_L) \\ &+ f_{\mu\tau}(\bar{\nu}_\mu^c\tau_L - \bar{\nu}_\tau^c\mu_L)] S - y_E\bar{E}E\Phi - M_E\bar{E}E \\ &- \sum_a^{e,\mu,\tau} y_a\bar{E}\ell_{Ra}S^\dagger - V(H, S, \Phi) + h.c.\end{aligned}$$

# The scalar Potential

The scalar potential  $V(H, S, \Phi)$  is

$$\begin{aligned} V = & -\mu^2 H^\dagger H + \lambda(H^\dagger H)^2 + M_S^2 S^\dagger S + \lambda_S(S^\dagger S)^2 \\ & + \lambda_{SH} S^\dagger S H^\dagger H + \lambda_\phi(\Phi^\dagger \Phi)^2 + M_\phi^2 \Phi^\dagger \Phi + \lambda_{\phi h} \Phi^\dagger \Phi H^\dagger H \\ & + \lambda_{\phi S} \Phi^\dagger \Phi S^\dagger S + \alpha \Phi + \beta \Phi^\dagger \Phi \Phi + \kappa_H \Phi H^\dagger H \\ & + \kappa_S \Phi S^\dagger S \end{aligned}$$

# Constraints from universality

- Exchange of  $S$  in muon decays will modify  $G_F$ . It interferes with SM
- Since new physics in the leptonic sector we assume unitarity of quark mixing and extract  $G_F$  from nuclear, Kaon and B-meson decays and compare with  $G_\mu$ . This gives

$$\mathcal{L} = \frac{if_{e\mu}^2}{2M_S^2} \left( \bar{\nu}_\mu \gamma^\alpha \hat{L} \nu_e \right) \left( \bar{e} \gamma_\alpha \hat{L} \mu \right)$$

whereas the SM has  $-\frac{ig^2}{2M_W^2}$  in front of the 4-fermi operator. Here

$$\hat{L} = (1 - \gamma_5)/2.$$

- We get

$$f_{e\mu} \leq 1.502 \times 10^{-1} \left( \frac{M_S}{400\text{GeV}} \right).$$

## $\tau$ leptonic decays

Use the leptonic  $\tau$  decays ratio into  $\mu, e$  we get

$$\begin{aligned}\frac{\Gamma(\tau \rightarrow \mu + \nu' s)}{\Gamma(\tau \rightarrow e + \nu' s)} &= \frac{\left(1 - \frac{f_{\mu\tau}^2 M_W^2}{g^2 M_S^2}\right)^2 + \dots}{\left(1 - \frac{f_{e\tau}^2 M_W^2}{g^2 M_S^2}\right)^2 + \dots} \\ &\simeq 1 + 2(f_{e\tau}^2 - f_{\mu\tau}^2) \left(\frac{M_W^2}{g^2 M_S^2}\right)\end{aligned}$$

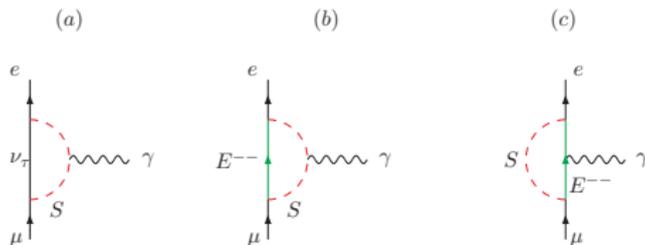
where  $\dots$  denotes terms such as  $f_{\mu e}^2 f_{\tau e}^2$  which come from diagrams that interfere incoherently with the SM ones. They are of order  $f^4$  which we neglect.

$$f_{e\tau}^2 - f_{\mu\tau}^2 \leq \pm 2.25 \times 10^{-2} \left(\frac{M_S}{400\text{GeV}}\right)^2.$$

Experimental value of  $\frac{\Gamma(\tau \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{\Gamma(\tau \rightarrow e^- \bar{\nu}_e \nu_\tau)} = 0.979 \pm 0.004$  has been used

$$\mu \rightarrow e + \gamma$$

The diagrams are



**Figure :** Diagrams leading to  $\mu \rightarrow e\gamma$ . Wavefunction renormalization graphs are not shown

Note that (a) has different chiral structure than (b) and (c) We get

$$f_{e\tau}^2 f_{\mu\tau}^2 + \left( \frac{y_e y_\mu X^2}{(1-x)^4} \right)^2 \left[ (-4 + 9x - 5x^3) + 6x(2x-1) \ln x \right]^2$$

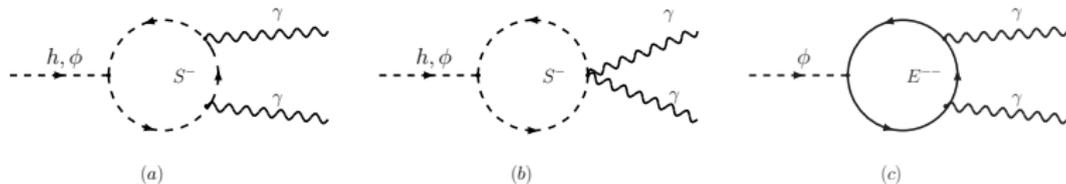
$$\leq 2.235 \times 10^{-12} \left( \frac{M_S}{400\text{GeV}} \right)^4,$$

where  $x = \frac{M_S^2}{M_E^2}$ .

- Similar diagrams yields constraint from anomalous magnetic moment of the muon,  $a_\mu$ .
- The constraint is not as strong as the above

# How do $E^{\pm\pm}$ and $S^pm$ held with $\phi$ signals?

Since we do not know the masses and first look at the case  $M_\phi < 2M_E(2M_S)$ .  
The signature is then the diphoton resonance



The effective Lagrangian is

$$\mathcal{L} = \frac{1}{f_\gamma} \phi (F_{\mu\nu})^2$$

The production is via photon fusion.

# Calculation of $f_\gamma$

$$f_\gamma^{-1} = \frac{\alpha}{4\pi M_\phi} \left( Q^2 N_{YE} \sqrt{\tau_E} F_{\frac{1}{2}}(\tau_E) + \frac{2(\lambda_\phi S W + \kappa_S)}{M_S} \sqrt{\tau_S} F_0(\tau_S) \right).$$

We define  $\tau_i = M_\phi^2/(4M_i^2)$  and the 1-loop functions are

$$F_0(\tau) = -[\tau - f(\tau)]\tau^{-2}; \quad F_{\frac{1}{2}}(\tau) = 2[\tau + (\tau - 1)f(\tau)]\tau^{-2}$$

with

$$f(\tau) = \begin{cases} \arcsin^2 \sqrt{\tau} & \tau \leq 1 \\ -\frac{1}{4} \left[ \log \frac{1+\sqrt{1-\tau^{-1}}}{1-\sqrt{1-\tau^{-1}}} - i\pi \right]^2 & \tau > 1. \end{cases}$$

From the limits of event rates for a 800 GeV  $\phi$  one can deduce that  $f_\gamma \sim 8 - 9$  TeV. The above give strong constraints on the model parameters since the  $F$  functions are known.

- $\kappa_S \ll v$ . The E-loop will be the dominant contribution. We obtain

$$y_E N \leq 16.8$$

where  $N$  is the number of  $E$ .

- $\kappa_S \gg v$  the  $S$  loop can assist. Then the constraint is

$$N y_E \sqrt{\tau_E} F_{\frac{1}{2}}(\tau_E) + \frac{\kappa_S}{2M_S} \sqrt{\tau_S} F_0(\tau_S) \lesssim 34$$

For  $\kappa_S \sim 10$  TeV the scalar loop dominates.

- di-boson widths

$$\begin{aligned}\Gamma_{\gamma\gamma} : \Gamma_{\gamma Z} : \Gamma_{ZZ} &= 1 : \frac{2s_w^2}{c_w^2} : \frac{s_w^4}{c_w^4} \\ &\approx 1 : 0.54 : 0.07 \\ \Gamma_{WW} &= 0.\end{aligned}$$

- Limits from  $h \rightarrow \gamma\gamma$

$$R = \left| 1 + \frac{\lambda_{SH} v^2}{2M_S^2} \frac{F_0(\tau')}{F_1(\tau_w) + \frac{4}{3}F_{\frac{1}{2}}(\tau_t)} \right|^2$$

where  $R \equiv \Gamma^{new} / \Gamma^{SM}$ ,  $\tau' = M_h^2 / 4M_S^2$  and  $F_1(\tau) = -[2\tau^2 + 3\tau + 3(2\tau - 1)f(\tau)]\tau^{-2}$ . The current bound on R is  $1.17 \pm 0.27$ . This yields the constraint:  $|\lambda_{SH}| < 8.1$ .

# Production of $E$ and $S$

- At hadron colliders  $S$  can be produced via Drell-Yan

$$q + \bar{q} \rightarrow S^+ S^- \rightarrow l^+ \nu l'^- \nu^c$$

The SM background is enormous

- For  $E$  we have

$$q + \bar{q} \rightarrow E + \bar{E} \rightarrow S^- + l_a^- + S^+ + l_b^+ \rightarrow l_a^- + l_c^- + l_b^+ + l_d^+ + \cancel{E}_T$$

where  $a, b, c, d$  denote the flavors of the charged leptons. Here the signal is four leptons plus  $\cancel{E}_T$  with no associated jets. Furthermore, the charged leptons do not form invariant mass peaks. Interestingly if the couplings  $f$ 's and  $y$ 's are very small i.e.  $< O(10^{-6})$  we will have displaced vertices.

- $e^+e^-$  colliders will be better since the signals are cleaner.

# Conclusions

- The singlet Higgs portal can have enhanced signals with the aid of vectorlike  $E^{\pm\pm}$
- Since  $E$  must not be stable a singlet charged scalar must be added
- The leading signal for the Higgs portal is  $\phi \rightarrow \gamma\gamma$ .
- $E$  and  $S$  will greatly enhanced this signal.
- Displayed vertices are important tools for these kind of new states.
- LHC can be very effective in probing very small couplings which to date are restricted to high precision low energy measurements.
- The best search for these are a high energy lepton collider